

ĐÁP ÁN ĐỀ THI CHÍNH THỨC

Câu	Ý	Nội dung	Điểm																																																						
1		<p>Ma trận hệ số ràng buộc</p> $A = \begin{pmatrix} 3 & 2 & 1 & 0 & 0 \\ 5 & 1 & 1 & 1 & 0 \\ 2 & 5 & 1 & 0 & 1 \end{pmatrix} \begin{matrix} 1 \\ 0 \\ 0 \end{matrix}$ <p>Thêm vào ẩn giả <math>x_6 \geq 0</math> ta được</p> $f(x) = x_1 + x_2 + x_3 + x_4 + x_5 + Mx_6 \rightarrow \min$ $\begin{cases} 3x_1 + 2x_2 + x_3 + x_6 = 1 \\ 5x_1 + x_2 + x_3 + x_4 = 3 \\ 2x_1 + 5x_2 + x_3 + x_5 = 4 \\ x_j \geq 0, \forall j = \overline{1,6} \end{cases}$	1,0																																																						
		<table border="1"> <thead> <tr> <th></th> <th></th> <th></th> <th><math>x_1</math></th> <th><math>x_2</math></th> <th><math>x_3</math></th> <th><math>x_4</math></th> <th><math>x_5</math></th> <th><math>\lambda_i</math></th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td></td> </tr> <tr> <td>M</td> <td><math>x_6</math></td> <td>1</td> <td>(3)</td> <td>2</td> <td>1</td> <td>0</td> <td>0</td> <td>1/3*</td> </tr> <tr> <td>1</td> <td><math>x_4</math></td> <td>3</td> <td>5</td> <td>1</td> <td>1</td> <td>1</td> <td>0</td> <td>3/5</td> </tr> <tr> <td>1</td> <td><math>x_5</math></td> <td>4</td> <td>2</td> <td>5</td> <td>1</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td></td> <td></td> <td></td> <td>3M+6*</td> <td>2M+5</td> <td>M+1</td> <td>0</td> <td>0</td> <td></td> </tr> </tbody> </table>				$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$\lambda_i$				1	1	1	1	1		M	$x_6$	1	(3)	2	1	0	0	1/3*	1	$x_4$	3	5	1	1	1	0	3/5	1	$x_5$	4	2	5	1	0	1	2				3M+6*	2M+5	M+1	0	0		1,0
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		Vậy phương án tối ưu là $x = \left(0, \frac{1}{2}, 0, \frac{5}{2}, \frac{3}{2}\right)$ và $f_{\min} = \frac{9}{2}$	1,0																																																						
		<b>Tổng cộng</b>	<b>5,0 đ</b>																																																						

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2		<p>Gọi <math>x_{ij}</math> là lượng hàng chuyển từ điểm kho <math>K_i</math> đến công trường <math>C_j, x_{ij} \geq 0</math>.</p> <p>Mô hình toán học:</p> $\min z(x) = 5x_{11} + 7x_{12} + 2x_{13} + 4x_{21} + 3x_{22} + 6x_{23} + 10x_{31} + 9x_{32} + 8x_{33} \quad (1)$ $\begin{cases} x_{11} + x_{12} + x_{13} = 10 \\ x_{21} + x_{22} + 6x_{23} = 40 \\ x_{31} + x_{32} + x_{33} = 10 \\ x_{11} + x_{21} + x_{31} = 15 \\ x_{12} + x_{22} + x_{32} = 20 \\ x_{13} + x_{23} + x_{33} = 25 \\ x_{ij} \geq 0 \quad (i = 1,2,3; j = 1,2,3) \end{cases}$	1,0																																								
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	<p>Ta có cước phí mới các ô không âm nên phương án cuối cùng là tối ưu.</p> <p>Kết quả của bài toán: <math>X = \begin{pmatrix} 0 &amp; 0 &amp; 10 \\ 15 &amp; 20 &amp; 5 \\ 0 &amp; 0 &amp; 10 \end{pmatrix}</math></p>	1,0																																									
	<p>Tổng số <math>T \times km</math> phải thực hiện là ít nhất: 250</p>	0,5																																									

Câu	Ý	Nội dung	Điểm
		<b>Tổng cộng</b>	<b>5,0 đ</b>